

Prediction of soil physical properties by optimized support vector machines

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A b s t r a c t. The potential use of optimized support vector machines with simulated annealing algorithm in developing prediction functions for estimating soil aggregate stability and soil shear strength was evaluated. The predictive capabilities of support vector machines in comparison with traditional regression prediction functions were also studied. In results, the support vector machines achieved greater accuracy in predicting both soil shear strength and soil aggregate stability properties comparing to traditional multiple-linear regression. The coefficient of correlation (R) between the measured and predicted soil shear strength values using the support vector machine model was 0.98 while it was 0.52 using the multiple-linear regression model. Furthermore, a lower mean square error value of 0.06 obtained using the support vector machine model in prediction of soil shear strength as compared to the multiple-linear regression model. The ERROR% value for soil aggregate stability prediction using the multiple-linear regression model was 14.59% while a lower ERROR% value of 4.29% was observed for the support vector machine model. The mean square error values for soil aggregate stability prediction using the multiple-linear regression and support vector machine models were 0.001 and 0.012, respectively. It appears that utilization of optimized support vector machine approach with simulated annealing algorithm in developing soil property prediction functions could be a suitable alternative to commonly used regression methods.

K e y w o r d s: soft computing, support vector machines, simulated annealing algorithm, soil shear strength, aggregate stability

INTRODUCTION

New soft computing techniques may be used in achieving tractability, robustness, and to provide a low cost solution with a tolerance of imprecision, uncertainty, partial truth, and approximation (Huang *et al.*, 2010). Among soft computing techniques, support vector machines (SVMs) have attracted greater interest recently in agricultural and biological engineering. SVMs are a promising machine learn-

ing method originally developed for pattern recognition problem based on structural risk minimization (Li *et al.*, 2009). Basically, SVMs are closely related to artificial neural networks (ANNs). In fact, SVM model using sigmoid kernel function is equivalent to a two-layer perceptron neural network. Using a kernel function, SVMs are alternative training methods for polynomial, radial basis function, and multilayer perceptron classifiers in which the weights of the network are found by solving a quadratic programming problem with linear constraints, rather than by solving a non-convex, unconstrained minimization problem as in standard ANN training (Huang *et al.*, 2010).

Choosing appropriate values for parameters of SVM is an important step in SVM analysis which has a great influence on its performance and thus on its prediction accuracy. In this sense, utilization of metaheuristics may be useful in discovering the optimal value of SVM parameters for the best forecast and estimation performance (Mo *et al.*, 2010; Zhang and Guo, 2009). Simulated annealing (SA) algorithm is one of the well-known metaheuristics that can discover a good quality solution to an optimization problem by trying random differences of the current solution (Kirkpatrick *et al.*, 1983). The original intension of SA is resemblance between annealing procedures of solid material in physics and general combination optimization problem and its application field is extended from the original combination optimizing problem to continuous space optimizing problem (Geng *et al.*, 2007; Kirkpatrick *et al.*, 1983).

Various laboratory-based techniques and indices have been proposed for measuring and evaluating the surface soil shear strength and soil aggregate stability. Nevertheless, most of these techniques are generally time consuming and rather complicated, particularly, when large amount of samples are required to be characterized for application on a large

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scale. Alternatively, these soil properties may be estimated using easily-available data by the use of soft computing techniques. Most commonly easily-available soil properties affecting soil shear strength and aggregate stability are soil particles, calcium carbonate, organic matter contents, and topographic attributes (Canasveras *et al.*, 2010; Canton *et al.*, 2009; Keşik *et al.*, 2010; Ohu *et al.*, 2009).

The main objective of this study was to investigate the potential use of an optimized SVM with SA algorithm in developing prediction functions for estimating soil aggregate stability and soil shear strength using easily-available soil properties.

Comparative evaluation of the predictive capabilities of SVMs and traditional regression prediction functions was also part of the goal.

MATERIALS AND METHODS

The study area was a part of Bazoft watershed (31° 37' to 32° 39' N and 49° 34' to 50° 32' E) located in northern part of Karun river basin in central Iran. A supervised random sampling was designed in different land unit tracts defined using geology, topography, and land use maps in the environment of ILWIS 3.4 software (ITC, University of Twente, Netherlands) to collect soil samples. A total of 160 soil samples were collected from the top 5 cm of soil surface to produce a measurement of diversity of soil properties within each land unit tracts. Soil organic matter (SOM) was determined by the Walkley-Black method (Nelson and Sommers, 1986). The analysis of soil particle size distribution *ie* very fine sand, fine sand, sand, clay, silt was performed using the procedure described by Gee and Bauder (1986). Calcium carbonate equivalent (CCE) was determined by the back-titration method (Nelson, 1982).

The soil samples for aggregate stability assessment were taken in such a way that minimum structural deformation and/or destruction happened to the soil aggregates. The method of van Bavel (1950) modified by Kemper and Rosenau (1986) was used to determine the wet-aggregate stability. Mean weight diameter (MWD) and geometric mean diameter (GMD) of the aggregates were used as indicators of soil aggregate stability. A shear vane (model: BS1377-9) was also used to measure the *in situ* surface soil shear strength (SSSS) in the saturation condition. The topographic attributes of the representative points including elevation, slope, and aspect were also characterized using a 20 by 20-m digital elevation model (DEM). For quantifying the vegetation in each representative point, the normalized difference vegetation index (NDVI) was derived using IRS-1D April 2008 satellite image at a spatial resolution of 24 by 24-m (Indian Space Applications Centre, Ahmedabad, India).

All the data were then tested for their normality using Kolmogorov-Smirnov method using SAS statistical software (Cary, NC., USA). Two different groups of easily-available inputs were selected for predicting soil aggregate

Table 1. Different inputs used for developing the SSSS and GMD prediction functions

Output	Inputs
SSSS	clay, silt, VFS, FS, sand, SOM, CCE, MWD, slop, aspect, NDVI, elevation
GMD	clay, silt, sand, SOM, CCE, slop, aspect, NDVI, elevation

VFS – very fine sand, FS – fine sand.

stability and soil shear strength (Table 1). Training set of 113 samples was obtained from total of 160 by random and the other 47 soil samples were used as the testing set.

Multiple-linear regression (MLR) was used for the regression analysis. The global regression model used in the data set was:

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \dots + \beta_n X_n, \quad (1)$$

where: Y is dependent variable, β_0 is a constant representing the Y value when all the independent variables are 0, X is independent variable, and $\beta_1, \beta_2, \beta_3, \dots, \beta_n$ are regression coefficients. The SAS statistical software was used to derive the multiple-linear regression models.

Support vector machines (SVMs) are the state-of-the-art neural network technology based on statistical learning (Vapnik, 1995). The basic idea of SVM is to use a linear model to implement non-linear class boundaries through non-linear mapping of the input vector into a high-dimensional feature space. The linear model constructed in the new space can represent a non-linear decision boundary in the original space.

Given a set of training data $D = \{(x_i, y_i)\}_{i=1}^n$ (where x_i is the input vector, $x_i \in X$, y_i is the desired value and $y_i \in R$, and n is the total number of data patterns), the regression function of SVM is formulated as follows:

$$y = f(x) = w_i \phi_i(x) + b, \quad (2)$$

where: ϕ_i is the feature of inputs, and w_i and b are coefficients. The coefficients (w_i and b) are estimated by minimizing the following regularized risk function (Vapnik, 1995):

$$r(C) = C \frac{1}{N} \sum_{i=1}^N l_\varepsilon(d_i, y_i) + \frac{1}{2} \|\omega\|^2, \quad (3)$$

where,

$$L_\varepsilon(d, y) = \begin{cases} |d - y| - \varepsilon & \text{if } |d - y| \geq \varepsilon \\ 0 & \text{otherwise} \end{cases}. \quad (4)$$

In Eq. (3), the first term is the empirical error (risk) and is measured by Eq. (4). The $L_\varepsilon(d, y)$ is called ε -insensitive loss function, the loss equals zero if the forecast value is within the ε -tube. The second term is used as a measure of

the flatness of the function. Thus, C is referred to the regularized constant and determines the trade-off between the empirical risk and the regularization term. The term ε is also the tube size and equivalent to the approximation accuracy placed on the training data points. Both C and ε are user-prescribed parameters, two positive slack variables ξ_i and ξ_i^* which represent the distance from actual values to the corresponding boundary values of ε -tube, are introduced. Then, Eq. (3) is transformed into the following constrained form:

$$\text{minimize: } \frac{1}{2} \|\omega\|^2 + C \sum_{i=1}^N (\xi_i + \xi_i^*), \quad (5)$$

$$\begin{aligned} \text{subject to: } & \omega_i \phi(x_i) + b_i - d_i \leq \varepsilon + \xi_i^*, \\ & d_i - \omega_i \phi(x_i) - b_i \leq \varepsilon + \xi_i, \\ & \xi_i, \xi_i^* \quad i=1, 2, \dots, N. \end{aligned}$$

This constrained optimization problem is solved using the following primal Lagrangian form:

$$\begin{aligned} L = & \frac{1}{2} \|\omega\|^2 + C \sum_{i=1}^N (\xi_i + \xi_i^*) - \sum_{i=1}^N a_i (\omega_i \phi(x_i) +), \\ & b - d_i + \varepsilon + \xi_i + \xi_i^*) - \sum_{i=1}^N a_i^* (d_i - \omega_i \phi(x_i) - b + \varepsilon + \xi_i^*) \\ & - \sum_{i=1}^N (\beta_i \xi_i + \beta_i^* \xi_i^*). \end{aligned} \quad (6)$$

Eq. (6) is minimized with respect to primal variables ω_i , b , ξ_i and ξ_i^* , and maximized with respect to the non-negative Lagrangian multipliers α_i^* and β_i^* . Finally, the Karush-Kuhn-Tucker conditions are applied to the regression, and Eq. (6) has a dual Lagrangian form:

$$\begin{aligned} v(\alpha_i, a_i^*) = & \sum_{i=1}^N d_i (\alpha_i, a_i^*) \\ -\varepsilon \sum_{i=1}^N (\alpha_i, a_i^*) - & \frac{1}{2} \sum_{i=1}^N \sum_{i=1}^N (\alpha_i, a_i^*) (\alpha_j, a_j^*) k(x_i, x_j), \end{aligned} \quad (7)$$

with the constraints of:

$$\sum_{i=1}^N (\alpha_i - \alpha_i^*) = 0 \quad \text{and } \alpha_i, \alpha_i^* \in [0, C], \quad i=1, 2, \dots, N. \quad (8)$$

In Eq. (7), the Lagrange multipliers satisfy the equality $\alpha_i, \alpha_i^* = 0$. The α_i and α_i^* are calculated, and the optimal desired weight vector of the regression hyper-plane is:

$$\omega^* = \sum_{i=1}^N (\alpha_i - \alpha_i^*) k(x, x_i). \quad (9)$$

Therefore, the regression function can be given as:

$$f(x, \alpha, \alpha^*) = \sum_{i=1}^N (\alpha_i - \alpha_i^*) k(x, x_i) + b. \quad (10)$$

Here, the $K(x_i, x)$ is named the kernel function. In this study, the radial basis function (RBF) was used as the kernel function:

$$K(x_i, x) = \exp\left(-\frac{\|x_i - x\|^2}{2\sigma^2}\right), \quad (11)$$

where σ is kernel parameter (Burgess, 1998; Cristianini and Taylor, 2000; Li *et al.*, 2009).

Discovering the optimal values of SVM parameters is important to achieve a good forecast and estimation performance (Mo *et al.*, 2010; Zhang and Guo, 2009). The simulated annealing (SA) algorithm was used for optimizing the parameters of SVM. More specifically, the SA executes the following steps (Geng *et al.*, 2007):

- choosing an initial solution and compute the value of the objective function of $F(x^{(0)})$;
- initializing the incumbent solution *ie* the best available solution, denoted by:

$$(x^*, F^*), \quad \text{as: } (x^*, F^*) \leftarrow (x^{(0)}, F(x^{(0)})). \quad (12)$$

- until a stopping criterion is fulfilled and for n starting from 0, do: draw a solution x at random in the neighborhood $V(x^{(n)})$ of $x^{(n)}$.

If $F(x) \leq F(x^{(n)})$ then $x^{(n+1)} \leftarrow x$ and if $F(x) \leq F^*$ then $(x, F(x))$.

If $F(x) > F(x^{(n)})$ then draw a number p at random in $[0, 1]$ and if $p \leq p(n, x, x^{(n)})$ then $x^{(n+1)} \leftarrow x$, else $x^{(n+1)} \leftarrow x^{(n)}$.

The function $p(n, x, x^{(n)})$ is often taken to be a Boltzmann function inspired from thermodynamics models:

$$p(n, x, x^{(n)}) = \exp\left(-\frac{1}{T_n} \Delta F_n\right), \quad (13)$$

where: $\Delta F = F(x) - F(x^{(n)})$ and T_n is the temperature at step n , that is a non-increasing function of the iteration counter n . In so-called geometric cooling schedules, the temperature is kept unchanged during each successive stage, where a stage consists of a constant number L of consecutive iterations. After each stage, the temperature is multiplied by a constant factor of $\alpha \in (0, 1)$.

In SA algorithm, if the candidate does not improve the current solution, there is still a possibility of transition according to the next probability function (Azizi and Zolfaghari, 2004):

$$P(\text{transition}) = \min\left\{1, \exp\left(-\frac{\Delta C_i}{\theta_i}\right)\right\}. \quad (14)$$

In each iteration, the above transition probability is compared with a uniform random number. If the probability value is greater than or equal to the random number, then the transition to the worse solution is accepted. If the transition from the current solution to the candidate solution is rejected, another solution in the neighborhood will be generated and evaluated. Due to the generalization of the concepts that it involves, the SA algorithm can be implemented to a wide range of optimization problems. In particular, no specific requirements are needed to be imposed neither on the objective function (derivability, convexity, *etc.*) nor on the solution space. Moreover, it can be shown that the meta-heuristic converges asymptotically to a global minimum (van Laarhoven and Aarts, 1988). Table 2 shows the optimal values of the SVM parameters resulting from SA analysis for the prediction of SSSS and GMD properties.

The mean square error (MSE), mean absolute error (MAE), correlation coefficient (R), and error percentage (ERROR%) between the measured and the predicted SSSS and GMD values were used to evaluate the performance of the proposed models. The MSE, MAE, and ERROR% statistics are defined as below:

$$\text{MSE} = \frac{1}{n} \sum_{k=1}^n [y_k - \hat{y}_k]^2 \quad (15)$$

$$\text{MAE} = \frac{1}{n} \sum_{k=1}^n [y_k - \hat{y}_k] \quad (16)$$

$$\text{ERROR \%} = \frac{\sum_{k=1}^n |y_k - \hat{y}_k|}{\sum_{k=1}^n y_k} 100 \quad (17)$$

where: \hat{y}_k denotes the predicted value y_k , is the measured value, and n is the total number of observations.

RESULTS AND DISCUSSION

The results on prediction of SSSS using MLR and SVM techniques are presented in Table 3. The MAE and MSE values for the MLR model were 0.81 and 0.99, respectively, and an ERROR% value of 12.72% found for this technique. A lower ERROR% value of 2.64% in prediction of SSSS using the SVM model obtained in comparison with the MLR model. The MAE and MSE values for the SVM model were also 0.17 and 0.06, respectively. The coefficient of correlation (R) between the measured and predicted SSSS values for the SVM model was 0.98 while it was 0.52 for the MLR model. Therefore, according to the evaluation indices, it appears that there is a more suitability of developing soil shear strength prediction models using SVM approach than traditional regression models. The worse performance of the

Table 2. Optimal values of the SVM parameters resulting from the simulated annealing algorithm analysis for the prediction of the SSSS and GMD properties

Soil property	SVM parameter		
	Kernel (σ)	Intensive (ϵ)	Punishment coefficient (C)
SSSS	0.1	0.09	18
GMD	0.5	0.06	24

Table 3. Goodness-of-fit of proposed MLR and SVM models for the prediction of soil shear strength

Model type	Evaluation criterion			
	MAE	MSE	R	ERROR %
MLR	0.81	0.99	0.52	12.72
SVM	0.17	0.06	0.98	2.64

Table 4. Goodness-of-fit of proposed MLR and SVM models for the GMD prediction

Model type	Evaluation criterion			
	MAE	MSE	R	ERROR %
MLR	0.08	0.012	0.42	14.59
SVM	0.02	0.001	0.97	4.29

MLR model in predicting the measured SSSS values can be also seen in Fig. 1, where the error performance values for the MLR model are more scattered than those for the SVM model. On the other hand, our findings also revealed the significance of combining soil properties with topographic and vegetation attributes together for the estimation of SSSS using the optimized SVM model with SA algorithm.

Table 4 shows the evaluation criterion results for the constructed MLR and SVM models for GMD prediction. The MAE, MSE, R, and ERROR% values for the GMD prediction using the MLR model were 0.08, 0.012, 0.42, and 14.59%, respectively. The SVM model could predict the GMD with more satisfactory performance than the MLR model and a higher correlation coefficient value of 0.97 was obtained for this technique as compared to that obtained by the MLR model. The MAE, MSE, and ERROR% values for GMD prediction using the SVM model were also 0.02, 0.001, and 4.29%, respectively. Higher error values in GMD prediction using the MLR method were also found in comparison with SVM method (Fig. 2). However, a similar trend of error performance values for GMD prediction using both techniques was observed for most of the samples. These results suggest a better performance of SVM technique in prediction of the GMD than MLR technique and thus

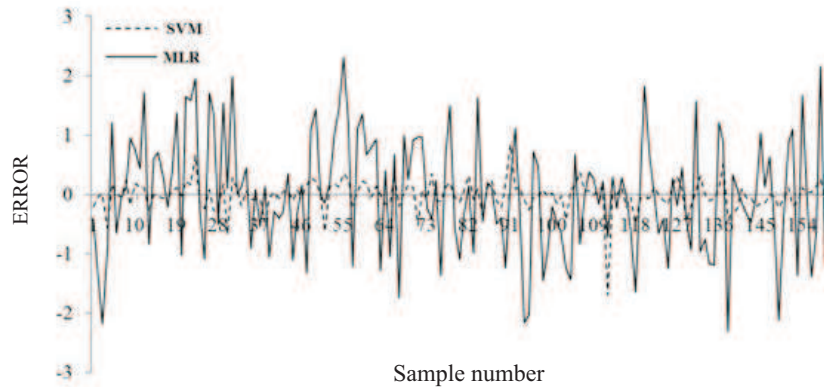


Fig. 1. Comparison of observed error values in SSSS prediction using SVM and MLR models.

the optimized SVM with SA algorithm technique seems to be more reliable in predicting the soil aggregate stability than MLR technique in the site studied.

Comparing the obtained results from the proposed MLR and SVM models indicated that the optimized SVM model with SA algorithm was better in predicting the investigated soil properties than the MLR model (Tables 3 and 4). The obtained coefficient of determination (R^2) values between the measured and the predicted SSSS and GMD values using both models also confirm this finding (Figs 3 and 4). The R^2 value between the measured and the predicted SSSS values using the MLR model was 0.27 while it was 0.95 using the SVM model (Fig. 3). Furthermore, the coefficient of determination values for the GMD prediction using the MLR and SVM models were 0.18 and 0.95, respectively (Fig. 4).

A reason for this finding (better performance of SVM approach in predicting the investigated soil properties) may be attributed to the less data available for developing reasonable MLR models. In contrast, the SVM models could recognize the relationships with relatively less data because

of their distributed and parallel computing nature. A second reason why the linear model *ie* multiple regression might be unreliable to predict the SSSS and GMD in the study area is that the effect of the predictors on the dependent variable may not be linear in the nature. In other word, the SVM models could probably predict the SSSS and GMD with more satisfactory performance owing to their more flexibility and capability to model non-linear relationships. In fact by using the kernel function in constructing of SVM model, the original inputs are first non-linearly mapped into the feature space, and the resulted ε -SVM becomes so flexible that it can be used to deal with the complicated non-linear regression problem (Li *et al.*, 2009). Furthermore, the low accuracy of the MLR approach in estimating the measured SSSS and GMD values might be associated with the sample distribution, spatial variation, and the study area scale effects. The major conceptual limitation of all regression techniques that is, one can only ascertain relationships but never be sure about underlying causal mechanism, should be also considered (Yilmaz and Yuksek, 2009).

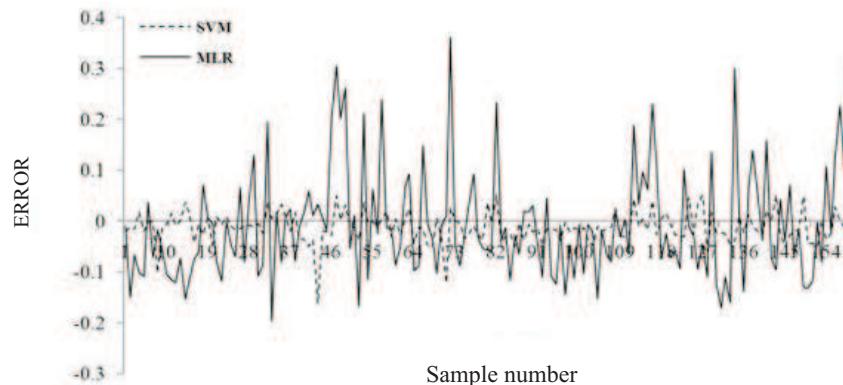


Fig. 2. Comparison of observed error values in GMD prediction using SVM and MLR models.

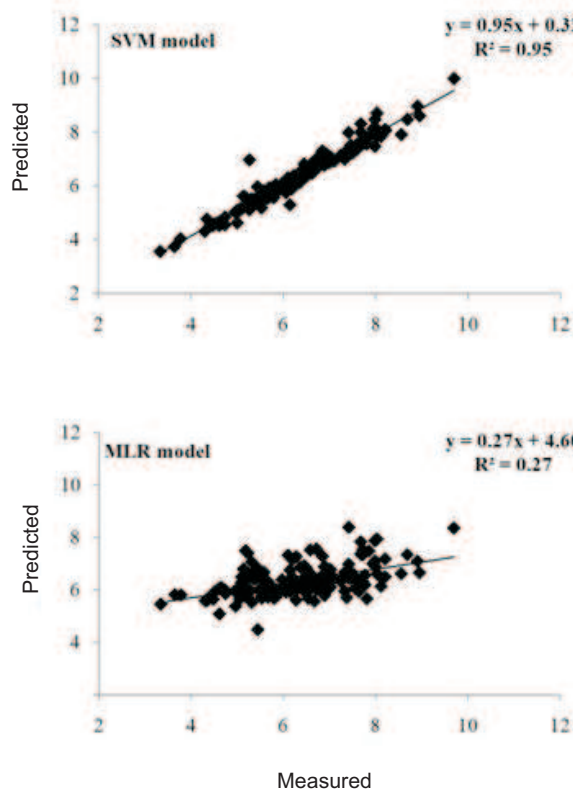


Fig. 3. Scatter plots displaying the relationships between measured and predicted values of SSSS using SVM and MLR models.

There are limited published studies dealing with the use of SVMs in soil sciences: Lamorski *et al.* (2008), for instance, estimated soil hydraulic parameters from measured soil properties using SVMs. They reported that 3-parameter SVMs performed generally better than or with the same accuracy as eleven parameter ANNs. Twarakavi *et al.* (2009) developed SVM models for estimating the hydraulic parameters describing the soil water retention and hydraulic conductivity. They stated that the SVM-based method predicted the hydraulic parameters better than the ANN-based method. Wang *et al.* (2009) compared different artificial intelligence methods for forecasting monthly discharge time series. They concluded that SVM model was able to obtain better forecasting accuracy in terms of the various evaluation measures during the both training and validation phases.

CONCLUSIONS

1. An optimized support vector machines with the simulated annealing algorithm was evaluated for predicting some soil properties *ie* soil shear strength and soil aggregate stability and achieved greater estimation accuracy comparable to that of traditional multiple-linear regression.

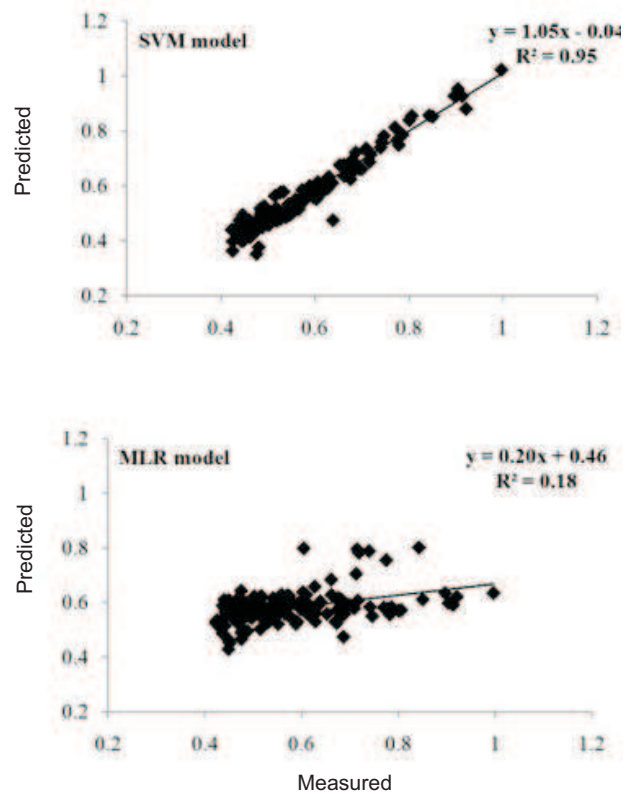


Fig. 4. Scatter plots showing the relationships between measured and predicted values of GMD using SVM and MLR models.

2. The effects of soil properties, topographic and vegetation attributes on soil shear strength and soil aggregate stability demonstrated the suitability of developing prediction functions using SVMs.

3. According to the advantages associated with the use of the SVM over traditional linear regressions, studies on this approach should continue in an effort to relate soil properties to the basic soil characteristics and its advantages should motivate soil scientists to work further on it in the future.

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